

## World Map

Mr. Pacha, a Bolivian archeologist, discovered an ancient document near Tiwanaku that describes the world during the Tiwanaku Period (300-1000 CE). At that time, there were  $N$  countries, numbered from 1 to  $N$ .

In the document, there is a list of  $M$  different pairs of adjacent countries:

$$(A[0], B[0]), (A[1], B[1]), \dots, (A[M-1], B[M-1]).$$

For each  $i$  ( $0 \leq i < M$ ), the document states that country  $A[i]$  was adjacent to country  $B[i]$  and vice versa. Pairs of countries not listed were not adjacent.

Mr. Pacha wants to create a map of the world such that all adjacencies between countries are exactly as they were during the Tiwanaku Period. For this purpose, he first chooses a positive integer  $K$ . Then, he draws the map as a grid of  $K \times K$  square cells, with rows numbered from 0 to  $K-1$  (top to bottom) and columns numbered from 0 to  $K-1$  (left to right).

He wants to color each cell of the map using one of  $N$  colors. The colors are numbered from 1 to  $N$ , and country  $j$  ( $1 \leq j \leq N$ ) is represented by color  $j$ . The coloring must satisfy all of the following **conditions**:

- For each  $j$  ( $1 \leq j \leq N$ ), there is at least one cell with color  $j$ .
- For each pair of adjacent countries  $(A[i], B[i])$ , there is at least one pair of adjacent cells such that one of them is colored  $A[i]$  and the other is colored  $B[i]$ . Two cells are adjacent if they share a side.
- For each pair of adjacent cells with different colors, the countries represented by these two colors were adjacent during the Tiwanaku Period.

For example, if  $N = 3$ ,  $M = 2$  and the pairs of adjacent countries are  $(1, 2)$  and  $(2, 3)$ , then the pair  $(1, 3)$  was not adjacent, and the following map of dimension  $K = 3$  satisfies all the conditions.

2	3	3
2	3	2
1	2	1

In particular, a country **does not** need to form a connected region on the map. In the map above, country 3 forms a connected region, while countries 1 and 2 form disconnected regions.

Your task is to help Mr. Pacha choose a value of  $K$  and create a map. The document guarantees that such a map exists. Since Mr. Pacha prefers smaller maps, in the last subtask your score depends on the value of  $K$ , and lower values of  $K$  may result in a better score. However, finding the minimum possible value of  $K$  is not required.

## Implementation Details

You should implement the following procedure:

```
std::vector<std::vector<int>> create_map(int N, int M,
    std::vector<int> A, std::vector<int> B)
```

- $N$ : the number of countries.
- $M$ : the number of pairs of adjacent countries.
- $A$  and  $B$ : arrays of length  $M$  describing adjacent countries.
- This procedure is called **up to 50 times** for each test case.

The procedure should return an array  $C$  that represents the map. Let  $K$  be the length of  $C$ .

- Each element of  $C$  must be an array of length  $K$ , containing integers between 1 and  $N$  inclusive.
- $C[i][j]$  is the color of the cell at row  $i$  and column  $j$  (for each  $i$  and  $j$  such that  $0 \leq i, j < K$ ).
- $K$  must be less than or equal to 240.

## Constraints

- $1 \leq N \leq 40$
- $0 \leq M \leq \frac{N \cdot (N-1)}{2}$
- $1 \leq A[i] < B[i] \leq N$  for each  $i$  such that  $0 \leq i < M$ .

- The pairs  $(A[0], B[0]), \dots, (A[M-1], B[M-1])$  are distinct.
- There exists at least one map which satisfies all the conditions.

## Subtasks and Scoring

Subtask	Score	Additional Constraints
1	5	$M = N - 1, A[i] = i + 1, B[i] = i + 2$ for each $0 \leq i < M$ .
2	10	$M = N - 1$
3	7	$M = \frac{N \cdot (N-1)}{2}$
4	8	Country 1 is adjacent to all other countries. Some other pairs of countries may also be adjacent.
5	14	$N \leq 15$
6	56	No additional constraints.

In subtask 6, your score depends on the value of  $K$ .

- If any map returned by `create_map` does not satisfy all the conditions, your score for the subtask will be 0.
- Otherwise, let  $R$  be the **maximum** value of  $K/N$  over all calls to `create_map`. Then, you receive a **partial score** according to the following table:

Limits	Score
$6 < R$	0
$4 < R \leq 6$	14
$3 < R \leq 4$	28
$2.5 < R \leq 3$	42
$2 < R \leq 2.5$	49
$R \leq 2$	56

## Example

In CMS, both of the following scenarios are included as part of a single test case.

### Example 1

Consider the following call:

```
create_map(3, 2, [1, 2], [2, 3])
```

This is the example from the task description, so the procedure can return the following map.

```
[  
  [2, 3, 3],  
  [2, 3, 2],  
  [1, 2, 1]  
]
```

## Example 2

Consider the following call:

```
create_map(4, 4, [1, 1, 2, 3], [2, 3, 4, 4])
```

In this example,  $N = 4$ ,  $M = 4$  and the country pairs (1,2), (1,3), (2,4), and (3,4) are adjacent. Consequently, the pairs (1,4) and (2,3) are not adjacent.

The procedure can return the following map of dimension  $K = 7$ , which satisfies all the conditions.

```
[  
  [2, 1, 3, 3, 4, 3, 4],  
  [2, 1, 3, 3, 3, 3, 3],  
  [2, 1, 1, 1, 3, 4, 4],  
  [2, 2, 2, 1, 3, 4, 3],  
  [1, 1, 1, 2, 4, 4, 4],  
  [2, 2, 1, 2, 2, 4, 3],  
  [2, 2, 1, 2, 2, 4, 4]  
]
```

The map could be smaller; for example, the procedure can return the following map of dimension  $K = 2$ .

```
[  
  [3, 1],  
  [4, 2]  
]
```

Note that both maps satisfy  $K/N \leq 2$ .

## Sample Grader

The first line of the input should contain a single integer  $T$ , the number of scenarios. A description of  $T$  scenarios should follow, each in the format specified below.

Input Format:

```
N M
A[0] B[0]
:
A[M-1] B[M-1]
```

Output Format:

```
P
Q[0] Q[1] ... Q[P-1]

C[0][0] ... C[0][Q[0]-1]
:
C[P-1][0] ... C[P-1][Q[P-1]-1]
```

Here,  $P$  is the length of the array  $C$  returned by `create_map`, and  $Q[i]$  ( $0 \leq i < P$ ) is the length of  $C[i]$ . Note that line 3 in the output format is intentionally left blank.